Computational Logic

Prolog Programming Basics

Overview

- 1. Using unification
- 2. Data structures
- 3. Recursion, backtracking, and search
- 4. Control of execution









```
date(day, date(Day,_Month,_Year),Day).
date(month,date(_Day,Month,_Year),Month).
date(year, date(_Day,_Month,Year),Year).
```

```
Accessing Data (Contd.)
 • Initializing variables:
   Example: ?- init(X), ...
   init(date(9,6,2011)).
 • Comparing values:
   Example: ?- init_1(X), init_2(Y), equal(X,Y).
   equal(X,X).
   or simply: ?- init_1(X), init_2(X).
```

Structured Data and Data Abstraction (and the '=' Predicate) • Data structures are created using (complex) terms. Structuring data is important: course(complog, wed, 18, 30, 20, 30, 'F.', 'Bueno', new, 5102). • When is the Computational Logic course? ?- course(complog,Day,StartH,StartM,FinishH,FinishM,C,D,E,F). Structured version: course(complog,Time,Lecturer, Location) :-Time = t(wed, 18:30, 20:30),Lecturer = lect('F.', 'Bueno'), Location = loc(new, 5102). **Note:** "X=Y" is equivalent to "=(X,Y)" where the predicate =/2 is defined as the fact "=(X,X)." – Plain unification! • Equivalent to: course(complog, t(wed, 18:30, 20:30), lect('F.', 'Bueno'), loc(new, 5102)).





- ◊ Base case: the empty list
- Recursive case: a pair (X,Y) where one argument is a list element and the other (usually the right one Y) is (recursively) a list (the rest of the list)
- Binary trees are basically records with a recursive structure in two arguments.

Lists

- Binary structure: first argument is *element*, second argument is *rest* of the list.
- We need:
 - ◊ a constant symbol: the empty list denoted by the *constant* []
 - ◊ a functor of arity 2: traditionally the dot "." (which is overloaded).
- Syntactic sugar: the term (X,Y) is denoted by [X|Y] (X is the *head*, Y is the *tail*).

Formal object	Cons pair syntax	Element s	yntax
.(a,[])	[a []]	[a]	
.(a,.(b,[]))	[a [b []]]	[a,b]	
.(a,.(b,.(c,[])))	[a [b [c []]]]	[a,b,c]	
.(a,X)	[a X]	[a X]	
.(a,.(b,X))	[a [b X]]	[a,b X]	
 Note that: 			
[a,b] and $[a X]$] unify with $\{X = [$	b]}	[a] and [a X] unify with {X = []}
[a] and [a,b X]] do not unify		[] and [X] do not unify



```
Lists (member)
 • member(X,Y) iff X is a member of list Y.
 • By generalization:
    member(a,[a]). member(b,[b]). etc. \Rightarrow member(X,[X]).
    member(a,[a,c]). member(b,[b,d]). etc. \Rightarrow member(X,[X,Y]).
    member(a, [a, c, d]). member(b, [b, d, 1]). etc. \Rightarrow member(X, [X, Y, Z]).
    \Rightarrow member(X, [X|Y]).
    member(a, [c,a]), member(b, [d,b]). etc. \Rightarrow member(X, [Y,X]).
    member(a,[c,d,a]). member(b,[s,t,b]). etc. \Rightarrow member(X,[Y,Z,X]).
    \Rightarrow member(X, [Y|Z]) :- member(X,Z).
 • Resulting definition:
   member(X, [X]]).
   member(X, [-|T]) := member(X, T).
```

```
Lists (member) (Contd.)

    Resulting definition:

   member(X, [X]]).
   member(X, [-|T]) := member(X, T).

    Uses of member(X,Y):

    checking whether an element is in a list: ?- member(b,[a,b,c]).

     ◊ finding an element in a list: ?- member(X, [a,b,c]).
     ◊ finding a list containing an element: ?- member(a,Y).
  • Define:
     ◇ select(X,Ys,Zs): X is an element of the list Ys and Zs is the list of the other
       elements of Ys.
     \diamond include(X,Ys,Zs) : Zs is the list resulting from including element X into list Ys
       (in any place).
                                                                                       14
```

```
Lists (append)
  • Concatenation of lists: append(X,Y,Z) iff Z = X.Y
   ("." is an operator for list concatenation)
  • By generalization (recurring on the first argument):
     ♦ Base case:
       append([],[a],[a]). append([],[a,b],[a,b]).
                                                            etc.
                                                               \Rightarrow append([],Ys,Ys).
     ◊ Rest of cases (first step):
       append([a],[b],[a,b]).
       append([a],[b,c],[a,b,c]). etc.
                                                        \Rightarrow append([X],Ys,[X|Ys]).
       append([a,b],[c],[a,b,c]).
       append([a,b],[c,d],[a,b,c,d]). etc.
                                                    \Rightarrow append([X,Z],Ys,[X,Z|Ys]).
      This is still infinite \rightarrow we need to generalize more.
                                                                                     15
```

```
Lists (append) (Contd.)
 • Second generalization:
   append([X],Ys,[X|Ys]).
   append([X,Z],Ys,[X,Z|Ys]).
   append([X,Z,W],Ys,[X,Z,W|Ys]).
                          \Rightarrow append([X|Xs],Ys,[X|Zs]) :- append(Xs,Ys,Zs).
 • So, we have:
   append([],Ys,Ys).
   append([X|Xs],Ys,[X|Zs]) :- append(Xs,Ys,Zs).
 • Uses of append:
    o concatenate two given lists: ?- append([a,b],[c],Z).

    find differences between lists: ?- append(X,[c],[a,b,c]).

    ◊ split a list: ?- append(X,Y,[a,b,c]).
```



```
Lists (reverse)
  • reverse(Xs,Ys): Ys is the list obtained by reversing the elements in the list Xs
  • Thinking computationally:
     ◊ It is clear that we will need to traverse the list Xs.
     ◇ For each element X of Xs, we must put X at the end of the rest of the Xs list
      already reversed:
             reverse([X|Xs],Ys) :-
                   reverse(Xs,Zs),
                   append(Zs,[X],Ys).
     ♦ How can we stop?
             reverse([],[]).
```

```
Lists (reverse) (and Accumulation Parameters)
As defined, reverse(Xs,Ys) is very inefficient.
Another possible definition:
reverse(Xs,Ys) :- reverse(Xs,[],Ys).
reverse([],Ys,Ys).
reverse([X|Xs],Acc,Ys) :- reverse(Xs,[X|Acc],Ys).
Find the differences in terms of efficiency between the two definitions.
```





```
Standard qsort (using append)
```

```
qsort([],[]).
qsort([X|L],SL) :-
    partition(L,X,Left,Right),
    qsort(Left,SLeft),
    qsort(Right,SRight),
    append(SLeft,[X|SRight],SL).
```

```
qsort w/Difference Lists (no append!)
 • First list is normal list, second is built as a difference list.
dlqsort(L,SL) :- dlqsort_(L,SL,[]).
dlqsort_([],R,R).
dlqsort_([X|L],SL,R) :-
        partition(L,X,Left,Right),
        dlqsort_(Left,SL,[X|SR]),
        dlqsort_(Right,SR,R).
% Partition is the same as before.
```









Senerate-and-Test Programs (II)
 <u>Example</u>: the N-queens problem
place N queens in an NxN chess board so that they do not attack each other
 Generate: NxN boards with N queens on them
Test: the queens on the board do not attack each other
<pre>queens(N,Board):- chess_board(N,Board), do_not_attack(Board).</pre>
• <u>Example</u> : play chess
 Generate: sequence of moves (of the two players) according to the rules of chess
Test: that the sequence leads to my victory!







White cuts: do not discard solutions.
max(X,Y,X):-X > Y, !. max(X,Y,Y):-X = < Y.
They affect neither completeness nor correctness – use them freely. (In many cases the system "introduces" them automatically.)
 Green cuts: discard correct solutions which are not needed.
address(X,Add):- home_address(X,Add), !. address(X,Add):- business_address(X,Add).
<pre>membercheck(X,[X Xs]):- !. membercheck(X,[Y Xs]):- membercheck(X,Xs).</pre>
They affect completeness but not correctness. Necessary in many situations (but beware!).

Types of Cut (Contd.)

• *Red* cuts: discard solutions which are not correct according to the intended meaning.

◊ Example:

```
\max(X,Y,X) := X > Y,!.
```

```
\max(X, Y, Y).
```

wrong answers to, e.g., $?- \max(5, 2, 2)$.

◊ Example:

```
days_in_year(X,366):- leap_year(X),!.
days_in_year(X,365).
```

```
wrong answers to, e.g., ?- days_in_year(a, D).
```

Red cuts affect completeness and one can no longer rely on the strict declarative interpretation of the program for reasoning about correctness – avoid when possible.

Using the Cut

Summary

- All that there is in logic programs is recursion and unification. (And backtracking.)
- Terms allow you to define any data structure and unification to manipulate it.
- Recursion allows you to program other control structures (with some help).
- Backtracking gives you the possibility to program search.
- Ordering of clauses, ordering of goals, and the cut are the only means to control execution.
- When designing programs, you can think of recursion in several ways.



